Lattice dynamics in the FeSi-based family of superconductors

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Abstract – The lattice dynamics of the superconducting materials LaFeSiH and LaFeSiO_{1- δ} as well as their intermetallic precursor LaFeSi are investigated by polarized Raman spectroscopy and first-principles calculations, together with X-ray and advanced electron diffraction techniques for their structural analysis. We find that the Fe-dominated Raman-active modes reflect the chemical peculiarities of these silicides compared to their pnictide counterparts, with enhanced structural couplings between the FeSi layer and the spacer that can be related to the ionic vs covalent character of the latter. In addition, we find signatures of enhanced electron-phonon coupling for some of the Raman-active modes. Beyond that, our study reveals intriguing Fe-based Raman features as well as structural subtleties in LaFeSiH suggesting that this superconductor may formally be non-centrosymmetric.

Introduction. – Iron-based superconductors provide a distinct realization of unconventional superconductivity [1,2] which, in some cases, can be supplemented with intriguing topological features [3,4]. These properties motivate a constant interest in new materials of this class. At present, there are only four successful compounds in which iron is combined with non-toxic crystallogen elements: the germanide YFe₂Ge₂ with superconducting $T_c \sim 0.1$ K [5–7] and the silicides LaFeSiH [8–10], LaFeSiF [11], and LaFeSiO with $T_c = 10$ K [12]. In the case of the silicides, some of their structure-property relationships challenge previous precepts such as the quasi-universal correlation between anion height and T_c thus calling for further investigations [12].

In this paper, we address the dynamical structural properties of the FeSi-based superconductors together with that of their LaFeSi precursor by means of polarized Raman spectroscopy combined with density-functionaltheory (DFT) calculations and advanced diffraction techniques. The measured phonon frequencies as well as the observed selection rules are found to be in good agreement with the calculations. In LaFeSiH, however, we observe a Raman Fe-based feature displaying an intriguing doublepeak shape. Driven by this observation, we revisit the crystal structure of this system by means of electron and X-ray diffraction. Furthermore, we elucidate the structural coupling between the FeSi layer and the LaX spacer in these systems from the trends of the phonon energies, which we discuss also in relation to the ionic vs covalent character of the spacer as a function of its precise composition (X = empty site, H, or O). In addition, the relative strength of the electron-phonon interaction is discussed from the Fano shape observed for some of the Ramanactive modes.

Methods. – Single crystals of the intermetallic LaFeSi were extracted from the bulk of an arc-melted sample with nominal composition $La_{35}Fe_{35}Si_{30}$. LaFeSiH single crystals were then obtained by hydrogenation of these crystals at 250°C under a gas flow of H₂ for 4h. Both the LaFeSi precursor and the LaFeSiH superconductor crystallize in the tetragonal ZrCuSiAs-type structure as confirmed from single-crystal X-ray diffraction. The samples have sub-millimeter size and a plate-like shape with the larger faces perpendicular to the crystallographic *c*-axis. The LaFeSiO samples, however, are from the same batch as Ref. [12], which displays an oxygen-site occupancy of ~ 0.9 and a T_c of 10 K. Specifically, they were obtained by heating powders of LaFeSi at 320 °C in 20%/80% O₂/Ar flow for 72 h. Microscopic crystals were then selected and the shiny faces were assumed to be parallel to the (001) plane as is the case for the other compounds. From these crystals we obtained well-defined polarized Raman spectra. However, the perfect orientation of the *a*-axis is lost in this case and hence the selection rules are almost fully (but not completely) obeyed.

The Raman spectra of small single crystals were measured under a microscope attached to a WITec (Model: alpha 300R) confocal Raman spectrometer. A 532 nm laser line was used for the excitation. The laser power was kept below 1 mW in order to avoid local overheating and/or damaging the crystals. Macro-Raman as a function of temperature was performed on a triple-stage spectrometer and in a cryo-free cryostat down to 9 K. Different polarizations of the light and orientations of the samples were investigated to access the symmetries of the excitations.

Precession electron diffraction tomography (PEDT) was performed with a JEOL F200 cold-FEG transmission electron microscope operated at 200 kV, equipped with a NANOMEGAS DigiStar precession module and a GATAN RIO16 camera. Samples for PEDT investigations were prepared by smoothly crushing powder. PEDT data was processed using the programs PETS 2.0 [13] and Jana2020 [14] (Cf. Suppl. Mat.).

The DFT calculations were performed with the Quantum ESPRESSO package [15] using the norm-conserving pseudopotentials from the PseudoDojo library [16]. We used the Perdew-Burke-Ernzerhof form of the generalized gradient approximation [17]. The calculations were converged with a Monkhorst-Pack mesh of $13 \times 13 \times 7 k$ -points and a 125 Ry cutoff for the wave functions with a 0.01 Ry smearing. We used the experimental lattice parameters reported in ref. [8,12,18] and optimized the internal coordinates of the La and Si atoms.

Preliminaries. – We first recall the nature of the Γ point phonons expected in our systems and their Raman selection rules. The systems under consideration represent the FeSi-based counterparts of previous 111 and 1111 Fe-based superconductors with P4/nmm crystal structure $(D_{4h}$ point group) [19]. The contribution of the different atoms to the different Γ -point phonons is summarized in Table 1. In the case of the LaFeSi precursor, we then have two A_{1g} , one B_{1g} and three E_g Raman-active modes. In LaFeSiH and LaFeSiO, there is an additional B_{1g} Ramanactive mode as well as another E_g mode.

In our experiments, the *c*-axis of the samples is parallel to Poynting vector of the light. The E_g modes, which are strongly affected by magnetism in BaFe₂As₂ [21], are not visible for this configuration. As a result, we then probe a total of $2A_{1g} + B_{1g}$ and $2A_{1g} + 2B_{1g}$ Ramanactive modes in LaFeSi and LaFeSiH/O, respectively, with

Table 1: Atoms and Γ -point phonons to which they contribute in LaFeSi and LaFeSiH/O. The Raman-active modes are indicated in bold.

Atom (Wyckoff position)	Γ -point modes
La $(2c)$	$\mathbf{A}_{1g} + \mathbf{A}_{2u} + \mathbf{E}_g + \mathbf{E}_u$
Fe $(2b)$	$\mathbf{B}_{1g} + \mathbf{A}_{2u} + \mathbf{E}_g + \mathbf{E}_u$
Si $(2c)$	$\mathbf{A}_{1g} + \mathbf{A}_{2u} + \mathbf{E}_{g} + \mathbf{E}_{u}$
H/O(2a)	$\mathbf{B}_{1g} + \mathbf{A}_{2u} + \mathbf{E}_g + \mathbf{E}_u$

Table 2: Raman selection rules for the D_{4h} point group in Porto's notation. a' stands for the (110) axis.

Polarization geometry	Raman-active phonons
$c(aa)\bar{c}$	$A_{1g}+B_{1g}$
$c(a'a')\bar{c}$	$A_{1g}+B_{2g}$
$c(ba)ar{c}$	$A_{2g}+B_{2g}$
$c(b'a')ar{c}$	$A_{2g}+B_{1g}$

selection rules as summarized in Table 2.

These modes are associated with out-of-plane displacements of the atoms. In the following, we denote these modes as $A_{1g}^{\text{La/Si}}$ and $B_{1g}^{\text{Fe/H/O}}$ according to the main contribution to these displacements. However, these modes generally have a mixed character with dominant and subdominant displacements of different atoms (Fe-X and Si-La).

LaFeSi precursor. – The Figure 1a) shows the polarized Raman spectra obtained on single crystals of the LaFeSi precursor at room temperature. The symmetry of the Raman-active phonons behind the observed peaks are deduced by changing the polarization geometry according to Table 2. We clearly identify the three modes A_{1g}^{La} , A_{1g}^{Si} , and B_{1g}^{Fe} . This identification is additionally supported by the DFT calculations (see Table 3), which also provide the main atomic character of these modes.

Superconducting LaFeSiH. – The polarized Raman spectra obtained from single crystals of LaFeSiH are shown in Figure 1b). In addition to the three modes A_{1g}^{La} , A_{1g}^{Si} , and B_{1g}^{Fe} , we observe the mode corresponding to B_{1g}^{H} . The frequencies of these modes are in reasonable agreement with the calculations (see Table 3), which again provide the main atomic character of these modes.

In the measured spectra, however, the B_{1g}^{Fe} mode at $\sim 228 \text{ cm}^{-1}$ appears as a double-peak feature. This is surprising because, even if this mode involves dominant Fe and subdominant H displacements, it should be a single non-degenerate mode. Accordingly, a symmetry breaking, for example, cannot produce such splitting. Furthermore, as shown in Fig. 2, no new modes or new splittings appear as a function of temperature and in none of the four



Fig. 1: Polarized Raman spectra of LaFeSi, LaFeSiH and LaFeSiO single crystals measured at room temperature. The configuration of the polarization is indicated in Porto's notation, with the selected Raman modes in bold. Black and red curves represent data from different samples. The insets show optical images of the samples. For LaFeSiO, star and losange symbols indicate a signal from the optical fiber in the setup and 'leakage' from A_{1g} modes, respectively, while circles indicate an additional high-energy feature, probably related to a multi-phonon process.

Table 3: Frequencies of the different Γ -point phonons of the investigated silicides together with their symmetries. In the case of the Raman-active modes observed in our experimental setup (i.e. A_{1g} and B_{1g}), the main atomic displacements are indicated with the superscripts.

LaFeSi		LaFeSiH		LaFeSiO				
Frequency	(cm^{-1})	Mode	Frequency	(\rm{cm}^{-1})	Mode	Frequen	$cy (cm^{-1})$	Mode
Experimental	Calculated	symmetry	Experimental	Calculated	symmetry	Exp.	Cal.	symmetry
	96	E_g		98	E_g		79	E_u
112.6	123	A_{1g}^{La}		115	E_u		106	A_{2u}
	148	E_u	146.4	120	A_{1q}^{La}		123	E_g
	152	A_{2u}		122	A_{2u}	164.4	156	B_{1q}^{Fe}
	209	E_g		178	E_g		179	E_g
205.6	218	B_{1q}^{Fe}	222.8, 228.5	228	B_{1q}^{Fe}	186	186	A_{1q}^{La}
250.0	313	A_{1g}^{Si}	279	289	A_{1g}^{Si}	_	272	$B_{1g}^{\check{\mathrm{O}}}$
	322	A_{2u}		315	A_{2u}		282	A_{2u}
	364	E_u		403	E_u		295	E_u
	372	E_g		407	E_g	260	297	A_{1q}^{Si}
			809.2	792	B_{1q}^{H}		389	A_{2u}
				809	E_u		414	E_g
				822	A_{2u}		414	E_u
				847	E_g		433	E_g

probed symmetries, which is consistent with the absence of a structural transition associated with magnetism re-



Fig. 2: Temperature dependence of the polarized Raman spectra on a third LaFeSiH single crystal, at 300 K, 100 K and 9 K. Spectra are shifted for clarity. The inset in a) shows that the distance between the maxima of the two-peak feature at 228 cm^{-1} is constant with temperature.

ported in [20]. The B_{1g} double-peak feature, however, persists down to 9 K as seen Fig. 2(a) and both the position of its two maxima and overall width remain quite constant. Note that the Raman inactive modes are relatively far in frequency from this feature (see Table 3), so that the Raman activation of some of these modes due to a structural change could hardly explain this observation (unless the change would be quite substantial).

The double-peak at ~ 228 cm⁻¹ is robust, in the sense that it is systematically observed in all the samples at the same frequency with similar relative intensities. Thus, even if the light only penetrates ~ 40 nm in this type of compounds, it should not be a surface artifact. In fact, the incomplete hydrogenation at the surface as well as a partial oxydation can be excluded by noting that the frequencies and FWHM of corresponding B_{1g} modes in the LaFeSi precursor and LaFeSiO (see below) are very different. Thus, we conclude that such a double-peak feature is LaFeSiH specific and has an intrinsic character.

However, according to the above, that feature cannot be easily explained within the P4/nmm structural model of LaFeSiH and hence questions the accuracy of such a



Fig. 3: Electron diffraction pattern obtained for LaFeSiH at the hk0 plane. The green circle indicates the 310 reflection expected according to the P4/nmm structure. The reflections encircled in red, however, are incompatible with *n*-glide plane symmetry. The Fourier-difference map obtained after the PEDT refinement is superimposed to the ball-and-stick model of the corresponding P4/nmm structure using VESTA [22]. This map shows residual densities close to Si sites (isosurface levels with $3\sigma[\Delta V(\mathbf{r})]$ are in yellow).

model. Thus, we used PEDT to carefully revisit the structure of this system. As explained in the Supplemental Material, the analysis of the PEDT data confirms the atomic positions and the site occupancies previously derived from X-ray diffraction [8]. However, it also reveals the presence of additional weak reflections as illustrated in Fig. 3, that suggests the absence of the *n*-glide plane symmetry. The PEDT refinement also displays a residual density close to the Si sites, if the P4/nmm structure is assumed. These observations thus confirm that the ideal P4/nmm model does not accurately capture all the structural details of the samples. To confirm the presence of these extra reflections, inferring that the actual structure would be non-centrosymmetric, we then performed additional single-crystal X-ray diffraction measurements.

However, due to their very weak intensity in both PEDT and X-ray diffraction, we could not determine the crystal structure of these systems more accurately. At the same time, we note that the extra reflections could also be due to the presence of stacking faults along c. In any case, the actual structure of these systems seems to be immeasurably close to P4/nmm while the Raman double-peak feature observed in LaFeSiH is visibly a much stronger effect. These observations then remain open questions.

Superconducting LaFeSiO. – The polarized Raman spectra obtained from LaFeSiO are shown in Fig. 1c). First, in the parallel polarized configuration we clearly observe two A_{1g} modes, at 187 cm⁻¹ and 260 cm⁻¹. The mode measured at 165 cm⁻¹ is assigned to the B_{1g}^{Fe} mode. In these measurements, however, the polarization of light with respect to the *a* axis is not perfect, so that there is no full extinction of the B_{1g} modes. Yet, we observe significant changes in the peak intensities from which the symmetry of the corresponding modes can be deduced. The relative intensity of the A_{1g} modes, for example, remains constant in parallel polarization when the polarization angle changes within the ab plane.

The B_{1g}^{O} mode is not immediately identifiable given the present data. This mode is expected at 272 cm⁻¹ according to our calculations and should be observable in the same configuration as the B_{1g}^{Fe} mode. We do observe intensity at 262 cm⁻¹ but it is more likely attributed to a "leakage" of the A_{1g}^{Si} (marked with a losange in Fig. 1), similarly to the "leakage" of the A_{1g}^{La} mode measured at about 182 cm⁻¹. In addition, a broad peak, marked with a circle, is measured at 672 cm⁻¹. It seems to be active in the A_{1g} channel. When considering leakage of E_g modes, the closest E_g mode is calculated to be at 433 cm⁻¹ and hence excludes such a possibility. In fact, there is no Γ point phonon matching that frequency. This high-energy feature may thus be related with a scattering process involving multiple phonons with finite wavevectors.

Comparative analysis. – To gain further insight about the structural properties of the above systems, we perform a comparative analysis in this section. The most relevant Raman features are summarized in Fig. 4 (see also Table 3).

First, we discuss the modes associated with the FeSi layer. We note that the frequency of the B_{1q}^{Fe} mode in LaFeSi and LaFeSiH is comparable to that of the reference compounds LaFeAsO (201 cm^{-1}) and SmFeAsO (208 cm^{-1}) reported in [23]. This mode, however, becomes considerably softer in LaFeSiO. This dynamical peculiarity adds to another, static one: a strikingly reduced distance between the Si and the Fe plane in this system [12]. Further, we note that the B_{1q}^{Fe} and A_{1q}^{As} modes are quasi degenerate in the above arsenides, while the frequencies of the B_{1g}^{Fe} and the A_{1g}^{Si} modes are quite different in the silicides with the latter being harder (also compared with the A_{1q}^{As} ones). The non-degeneracy of these modes suggests that the structural coupling of the FeSi layer to the spacer is more important in the silicides. The above trends are confirmed in the calculations.

Next, we discuss the modes associated with the spacer. The A_{1g}^{La} becomes progressively harder from LaFeSi, to LaFeSiH then to LaFeSiO. This can be related to the insertion of the light element within the spacer and its electronegativity. The observed trend then suggests that the ionic character of the spacer increases with increasing electronegativity of the inserted element, thereby hardening the A_{1g}^{La} mode. At the same time, we also note that the frequency of this mode in LaFeSiO is higher compared to that in LaFeAsO. This can be associated with the subdominant contribution of the Si displacements, which again suggests an enhanced structural coupling between the FeSi layer and the spacer. Since this is eventually determined by the corresponding chemical bonds, the electronic structure of these silicides can be expected to be more three-



Fig. 4: Experimental Raman spectra of (a) LaFeSi, (b) LaFeSiH and (c) LaFeSiO as measured at T = 300 K. The theoretically calculated positions of the phonon modes are marked below the data as ticks and arrows for the non-degenerate and degenerate modes, respectively. The insets show the Raman features associated with the B_{1g}^{Fe} mode, whose fitting requires two peaks in LaFeSiH.

Table 4: Fano parameter $10^3 \cdot \frac{1}{q^2}$ for the two A_{1g} modes mainly associated with La and Si. The corresponding fits are shown in Fig. 3 of the Supplementary Material. The higher $\frac{1}{q^2}$, the stronger the Fano effect is.

	$\mathbf{A}_{1g}^{\mathrm{La}}$	$\mathbf{A}_{1g}^{\mathrm{Si}}$
LaFeSi	32(3.4)	11(2.1)
LaFeSiH	3.5(0.8)	3.5(0.4)
LaFeSiO	27(4.4)	2.1(0.4)

dimensional in general with low-energy details near the Fermi level more sensitive to changes in the spacer.

Finally, we note that, in general, the A_{1g} Raman peaks in the silicides display a Fano shape that is more apparent compared to their arsenide counterparts [23] (see Table 4). In addition, we observe a significant broadening of the A_{1g}^{La} mode from 5 cm⁻¹ in the LaFeSi precursor to ~ 10.5 cm⁻¹ in LaFeSiH and LaFeSiO.

These differences can be due to enhanced electronphonon couplings for these particular Γ -point modes. In relation to superconductivity, however, the most relevant couplings involve the Fe-dominated modes and, in any case, the strength of the overall coupling according to DFT calculations remains too weak to explain the superconducting T_c of LaFeSiH for example [24].

Conclusion. – Our combined analysis of the lattice dynamics of Fe-based superconducting silicides reveals that, compared with their arsenide counterparts, the structural coupling between the FeSi layer and the spacer is stronger. This dynamics is also found to be affected by the change from covalent to more ionic bonds within the spacer across the LaFeSiX series (X = empty site, H, and O). Consequently, despite their layered structure, the effective 2D behavior is different in these systems. Intriguingly, the Raman spectrum of LaFeSiH displays a doublepeak feature that cannot be easily explained according to the ideal P4/nmm crystal structure of these systems. Besides, detailed electron and X-ray diffraction suggests that the structure may in reality be non-centrosymmetric. Thus, it would be interesting to determine the structure of these systems more accurately and, if the absence of centrosymmetry is confirmed, to further investigate the superconducting properties of Fe-based silicides from that perspective.

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Contributions: MAM conceived the work and supervised the project with AC. JBV and ST synthetized the LaFeSi(H) samples and performed XRD measurements. MH and PT synthetized LaFeSiO. PB performed and analysized the PEDT measurements. SL and MH performed the Raman experiments with the support of MAM. AC performed the ab-initio calculations. MAM, AC and MH discussed the results and wrote the manuscript, with contributions from all the authors.

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