

$$1 \quad \psi = e^{ikz} + A e^{-ikz}$$

$$\psi' = ik e^{ikz} - A ik e^{-ikz}$$

$$\text{en } z=0$$

$$\psi = 1 + A$$

$$\psi' = ik [1 - A]$$

$$2 \quad \psi = B e^{\alpha z} + C e^{-\alpha z}$$

$$\psi' = \alpha B e^{\alpha z} - \alpha C e^{-\alpha z}$$

$$\text{en } z=0$$

$$\psi = B + C$$

$$\psi' = \alpha [B - C]$$

$$\text{en } z=d$$

$$\psi = B e^{\alpha d} + C e^{-\alpha d}$$

$$\psi' = \alpha [B e^{\alpha d} - C e^{-\alpha d}]$$

$$3 \quad \psi = D e^{ik(z-d)}$$

$$\psi' = ik D e^{ik(z-d)}$$

$$\text{en } z=d$$

$$\psi = D$$

$$\psi' = ik D$$

$$1 + A = B + C$$

$$ik [1 - A] = \alpha [B - C]$$

$$B e^{\alpha d} + C e^{-\alpha d} = D$$

$$\alpha [B e^{\alpha d} - C e^{-\alpha d}] = ik D$$

$$ik [2 - B - C] = \alpha [B - C]$$

$$B [ik + \alpha] = 2ik + C [d - ik]$$

$$C = D e^{\alpha d} - B e^{-2\alpha d}$$

$$\alpha [B e^{\alpha d} - C e^{-\alpha d}] = ik D$$

$$\left. \begin{aligned} B [ik + \alpha] &= 2ik + (\alpha - ik) \\ \alpha [B e^{\alpha d} - D + B e^{-\alpha d}] &= ik D \end{aligned} \right\} D e^{\alpha d} - B e^{-\alpha d} \left. \right\}$$

$$2B \alpha e^{\alpha d} = D (ik + \alpha)$$

$$D [ik + \alpha]^2 = 2ik \alpha e^{\alpha d} + [\alpha - ik] \\ \times 2 \alpha e^{-\alpha d} D - e^{-\alpha d} (ik + \alpha) \left. \right\}$$

$$D \{ [\alpha + ik]^2 - [\alpha - ik]^2 \} 2\alpha - ik - \alpha \left. \right\} e^{-\alpha d} \\ = 4ik \alpha e^{-\alpha d}$$

$$D \{ (\alpha + ik)^2 - (\alpha - ik)^2 \} e^{-\alpha d} \left. \right\} = 4ik \alpha e^{-\alpha d}$$

$$D = \frac{4\alpha d}{(\alpha + ik)^2 e^{-\alpha d} - (\alpha - ik)^2 e^{\alpha d}}$$

$$= \frac{4\alpha d}{2(\alpha^2 - k^2) \sinh \alpha d + 4ik \cosh \alpha d}$$

$$= \frac{1}{\cosh \alpha d + \frac{\alpha^2 - k^2}{2ik\alpha} \sinh \alpha d}$$

$$|D|^2 = \frac{1}{\cosh^2 \alpha d + \frac{(\alpha^2 - k^2)^2}{4\alpha^2 k^2} \sinh^2 \alpha d}$$

$$= \frac{1}{1 + \left[1 + \frac{(\alpha^2 - k^2)^2}{4\alpha^2 k^2} \right] \sinh^2 \alpha d}$$

$$= \frac{1}{1 + \frac{\alpha^2 + k^2}{4\alpha^2 k^2} \sinh^2 \alpha d}$$